# Applying yourself to <br> Environmental data 

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## the Apply family

## applies functions to parts of data

- array data:
- apply
- tapply $\rightarrow$ aggregate
- outer
- List data:
- lapply and friends:
- sapply, mapply, vapply,
- replicate
- rapply, dendrapply
- eapply


## Let's get some data

- Temps - a matrix of temperatures no various dates (rows) at different stations (columns)

$$
\begin{array}{lrrr} 
& \text { Island } & \text { Barrie } & \text { YYZ } \\
\text { winter } & -4 & -12 & -5 \\
\text { spring } & 8 & 6 & 9 \\
\text { summer } & 29 & 28 & 31 \\
\text { fall } & 19 & 15 & 20
\end{array}
$$

## find the mean temperatures in:

- each season, across sites;
- each site, across seasons.
- Now, find the median temperatures


## apply applies a function to columns or rows

- apply(Temps,1,mean) \# row means
- apply(Temps,2,mean) \# column means
- apply(Temps,1,median) \# row medians
- apply(Temps,2,sd) \# col. standard deviations


## apply applies your function to columns or rows

- apply(Temps,2,function(x)\{median(x)mean(x)\})
- apply(Temps,2,function(x)\{x-mean(x)\} )
- \# what happens here?


## apply applies a function to arrays as well

apply(TempsYrly,1,median) \#
apply(TempsYrly,2,median) \#
apply(TempsYrly,3,median) \#

## robust scaling

robustScale<-function(x)\{(x-median(x)/(IQR(x)/2)\} \# like scale, but uses median instead of mean, and \# Inter-quartile Range instead of sd
r<-rnbinom(n=10000,mu=10,size=2) \# nice skewed data hist(r)
histr<-function(x,brks=50,...)\{hist(x,breaks=brks,col="black",...)\} histr(r) \# nice convenience function to have histr(scale(r),brks=20) \# compare with: histr(robustScale(r) ,brks=20,xlab="number in quadrat")

## some serious data

- a 20 million year BP series of CO2 and Northern hemisphere mean temperatures
- Graversen RG, Drijfhout S, Hazeleger W, van de Wal R, Bintanja R, Helsen M. Greenland's contribution to global sea-level rise by the end of the 21st century. Climate dynamics. 2011;37(7-8):1427-42.
r<-CO2_NHtemp[CO2_NHtemp\$time> -2e3,] \# last 2 Myrs
with(r,plot(dTNH,CO2ppm))
with(r,plot(time,CO2ppm))
t10K<-floor(r\$time/10) \# 10,000 year lumps
z<-apply(r[,2:3],2,robustScale); z<-aggregate(z, by=list(t10K=t10K),median)
plot(z\$t10K,CO2ppm,ty="l",lty=1,col="blue",xlab="time BP (10,000 year units)",ylab="robust $z$-score")
lines(z\$t10K,z\$dTNH,col="red")


## mapply - apply a function with multiple arguments

- result <- mapply(function, arg1, arg2...argN,moreArgs)
- mapply(rep, 1:4, 4:1)
- mapply(rep, times $=1: 4, x=4: 1$ )
- netPP<-
function(temp,CO2,alpha=0,beta=1)\{temp*beta*(CO2-alpha)\}
- $x=m a p p l y(n e t P P, z \$ d T N H, z \$ C O 2 p p m) ;$ plot( $x$, ty="I", xlab="time",ylab="NPP")
- $x=m a p p l y(n e t P P, z \$ d T N H, z \$ C O 2 p p m, a l p h a=-2, b e t a=.5)$; lines(x,col="red")


## with multi-dimensional arrays more fun is possible

apply(TempsYrly,1:2,median) \# median how? apply(TempsYrly,2:3,median) \# when? apply(TempsYrly,c(1,3),median) \# where?

## a bit of visualization

overYears<-apply(TempsYrly,c(1,2),median)
cols<- rev(rainbow(24, start $=0$, end $=.6)$ )
heatmap(overYears ,col=cols,
Rowv=NA,Colv=NA,scale="none",cexCol=1.2)


## tapply $\rightarrow$ aggregate

## groups <- as.factor(rbinom(32, $\mathrm{n}=16$, prob $=$

 0.4))> tapply(groups, groups, length) \#- is almost the same as
710111213141516
12122125
$>$ tabulate(groups)
[1] 12122125

## tapply $\rightarrow$ aggregate

- tapply(data, factors, FUN = myFunction)
- use when we want to group the data by one or more factors before summarizing each group using
- each group is all the data having a specific combination of values of each of the factors supplied
- use with "ragged" data that doesn't fit easily in an array


## tapply - a simple example

## fishSites

| "Smoke" | "Cache" | "Cache" | "2Rivers" | "Rock" | "Smoke" |
| :--- | :--- | :--- | :--- | :--- | :--- |
| "Cache" | "Opeongo" | "Opeongo" | "Canoe" | "Smoke" | "Opeong |
| "Cedar" | "Grand" | "Rock" | "Grand" | "Smoke" | "Sec" |
| "Grand" | "Grand" | "Rock" | "Mud" | "Opeongo" | "2River |
| "Opeongo" "Canoe" | "Mud" | "Mud" | "Mud" | "Opeong |  |
| tapply(fishSiteS, fishSiteS, length) |  |  |  |  |  |
| 2Rivers Cache Canoe Cedar Grand | Mud Opeongo Rock Sec Smoke |  |  |  |  |
| 2 | 3 | 2 | 1 | 4 | 4 |
| 4 | 3 | 1 | 4 |  |  |

\# fishSites is both data, and the factor we group on

## aggregate instead of tapply

- result<- aggregate(data,by=listOfFactors, function)
- ft1<-tapply(fishCatch\$temp,fishCatch[,1:2],mean)
- ft2<-aggregate(fishCatch\$temp, by=list(where=fishCatch \$sites, when=fishCatch\$season), mean)
- ft3<-aggregate(fishCatch\$temp, by=fishCatch[,1:2], mean)
- ft4<-aggregate(fishCatch\$temp, by=list(when=fishCatch \$season, where=fishCatch\$sites), mean)
- ft5<-aggregate(fishCatch\$temp, by=fishCatch[,2:1], mean)
- ft6<-aggregate(fishCatch[,3:4], by=fishCatch[,2:1], mean)
- Compare these. Where are they the same, where different?


## What is N for tapply/aggregated data?

- ft6n<-aggregate(fishCatch[,3:4], by=fishCatch[,2:1], length)
- ft6nt<-tapply(fishCatch[,3], fishCatch[,2:1], length)
- How are these different? where might you use this?


## going to "outer" space

- outer is very cool. Make yourself into an R astronaut by using outer space...
- result<-outer(x,y,myFunction)
- returns array with as many rows as $x$, columns as $y$, and result $[i, j]==m y F u n c t i o n(x[i], y[j])$
- classic example: $x=1: 9$; multTable=outer( $x, x,{ }^{\prime *}{ }^{* \prime \prime}$ )
- note if using a built-in R function such as +-*/ etc, put it in quotes
- if using a named function (Alex, where are you????) no quotes


## what is the closest point in outer space?

- you measured many environmental variables at lots of sampling points.
- Each sampling point has an $x$ and $y$ coordinate (in meters, km, $10^{\text {th }}$ century king's feet, etc)
- You've got a dataframe EnvDat with columns $x, y$, and $N$ more columns for your $N$ environmental measures (e.g. noon temp, soil carbon, \% canopy cover)
myXY is a dataframe of points within the experimental site Let's find closest 3 points in EnvDat to each X,Y point. d<-sqrt(outer(myXY\$x,EnvDat\$x,"-"-")^2 + outer(myXY\$y,EnvDat\$y,"-")^2) s<-apply(d,1,order)[,1;3]
\# not shown: we could now interpolate weighted noon temp, soil carbon, etc from these 3 nearest points in EnvDat


## lists are for ragged data

- matrices, arrays all need same number of entries in rows, columns.
- in the real world you may have different numbers of observations at different sites
- lists are for you!
- the $\mathrm{i}^{\text {th }}$ member of a list L is $\mathrm{L}[[i]]$
- look at variable sites3


## sapply applies functions within lists, then simplifies the result

- sapply(sites3,mean)
- sapply(sites3,sd)
- sapply(sites3,function $(x)\{c(m=m e a n(x), s=s d(x))\}$
- sapply(sites3,quantile,seq(.2,.8,.1) )


## lapply doesn't simplify

- lapply(sites3,mean)
- lapply(sites3,robustScale)


## replicate for simulation

- replicate(n_times, expression)
- replicate(3,rnorm(2,0,1))
- replicate(3,rnorm(sample(10,1),0,1))


## for another time: recursive applies

- rapply recursively applies a function down the levels of a list, most often one representing something like a tree or graph structure
- dendryapply does this to dendrogram objects produced by various clustering methods


## THANKS!

## a less elementary example, Watson!

- you have latitude of your observation sites and the date. How long was the day?
- in Wikipedia, you find the sunrise equation: $-\cos (w)=-\tan (\mathrm{L}) * \tan (\mathrm{D})$
- instantly, you achieve enlightenment, quit graduate school, and start your own cult
- or perhaps you actually want to know the day length, poor unenlightened you!


## the Outer space solution

- $\operatorname{tanL}=\tan ($ LatToR(lat) $)$
- tanD $=\tan ($ SunDecl(day,lat))
- cosw = - outer(tanL,tanD, "*")
- hours $=2$ * RadToHour(arccos(cosw))
- check it: dataframe DaySites has lat, day of year


## the $R$ sunrise equation

- L is Latitude in radians (Alex, how do we convert from Google Maps latitudes to radians? help!!!)
- D is the sun declination (how much is the sun at noon above where is would be on March 21, in radians...help!!!)
- w is the "hour angle" in radians
- daylength (hours) $=2$ * w/ 15


## solving the sunrise equation

- you and Alex make a function LatToR(lat) to convert latitude in degrees (like 45.1278) to radians
- you and Alex make another function SunDecl(day, lat) to convert day of the year (measured from 1=Jan 1) and latitude into sun declination
- you and Alex make a function to convert back from radians into hours....RadToHour(rads)
- now, you are ready to rock and roll!

